

Q1. Match List - I with List - II.

List - I (Number)

List - II (Significant figure)

(A) 1001 (I) 3

(B) 010.1 (II) 4

(C) 100.100 (III) 5

(D) 0.0010010 (IV) 6

Choose the correct answer from the options given below:

(1) (A)-(III), (B)-(IV), (C)-(II), (D)-(I)

(2) (A)-(IV), (B)-(III), (C)-(I), (D)-(II)

(3) (A)-(II), (B)-(I), (C)-(IV), (D)-(III)

(4) (A)-(I), (B)-(II), (C)-(III), (D)-(IV)

Q2. Train A is moving along two parallel rail tracks towards north with 72 km h^{-1} and train B is moving towards south with speed 108 km h^{-1} . Velocity of train B with respect to A and velocity of ground with respect to B are (in m s^{-1}):

(1) -30 and 50

(2) -50 and -30

(3) -50 and 30

(4) 50 and -30

Q3. A cricket player catches a ball of mass 120 g moving with 25 m s^{-1} speed. If the catching process is completed in 0.1 s then the magnitude of force exerted by the ball on the hand of player will be (in SI unit):

(1) 24

(2) 12

(3) 25

(4) 30

Q4. A body of mass 4 kg experiences two forces $\vec{F}_1 = 5\hat{i} + 8\hat{j} + 7\hat{k}$ and $\vec{F}_2 = 3\hat{i} - 4\hat{j} - 3\hat{k}$. The acceleration acting on the body is:

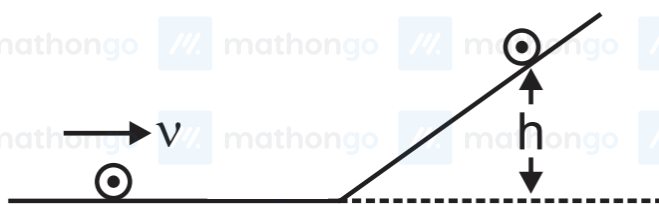
(1) $-2\hat{i} - \hat{j} - \hat{k}$

(2) $4\hat{i} + 2\hat{j} + 2\hat{k}$

(3) $2\hat{i} + \hat{j} + \hat{k}$

(4) $2\hat{i} + 3\hat{j} + 3\hat{k}$

Q5. A disc of radius R and mass M is rolling horizontally without slipping with speed v . It then moves up an inclined smooth surface as shown in figure. The maximum height that the disc can go up the incline is:



(1) $\frac{v^2}{g}$

(2) $\frac{3v^2}{4g}$

(3) $\frac{1v^2}{2g}$

(4) $\frac{2v^2}{3g}$

Q6. A light planet is revolving around a massive star in a circular orbit of radius R with a period of revolution T . If the force of attraction between planet and star is proportional to $R^{-3/2}$ then choose the correct option :

(1) $T^2 \propto R^{5/2}$

(2) $T^2 \propto R^{7/2}$

(3) $T^2 \propto R^{3/2}$

(4) $T^2 \propto R^3$

Q7. A big drop is formed by coalescing 1000 small droplets of water. The surface energy will become :

(1) 100 times

(3) $\frac{1}{100}$ th

(2) 10 times

(4) $\frac{1}{10}$ th

Q8. A diatomic gas ($\gamma = 1.4$) does 200 J of work when it is expanded isobarically. The heat given to the gas in the process is :

(1) 850 J

(3) 600 J

(2) 800 J

(4) 700 J

Q9. If the root mean square velocity of hydrogen molecule at a given temperature and pressure is 2 km s^{-1} , the root mean square velocity of oxygen at the same condition in km s^{-1} is:

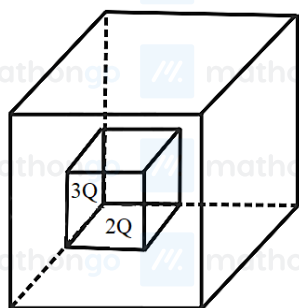
(1) 2.0

(3) 1.5

(2) 0.5

(4) 1.0

Q10. C_1 and C_2 are two hollow concentric cubes enclosing charges $2Q$ and $3Q$ respectively as shown in figure. The ratio of electric flux passing through C_1 and C_2 is:



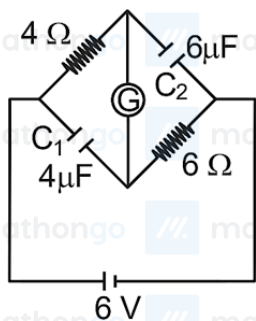
(1) 2 : 5

(3) 2 : 3

(2) 5 : 2

(4) 3 : 2

Q11. A galvanometer G of 2Ω resistance is connected in the given circuit. The ratio of charge stored in C_1 and C_2 is:

(1) $\frac{2}{3}$

(3) 1

(2) $\frac{3}{2}$ (4) $\frac{1}{2}$

Q12. In a metre-bridge when a resistance in the left gap is 2Ω and unknown resistance in the right gap, the balance length is found to be 40 cm. On shunting the unknown resistance with 2Ω , the balance length changes by:

(1) 22.5 cm

(3) 62.5 cm

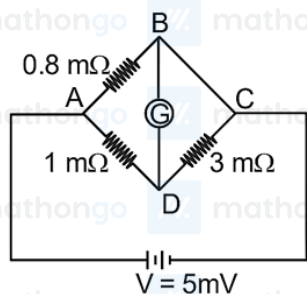
(2) 20 cm

(4) 65 cm

Q13. In an ammeter, 5% of the main current passes through the galvanometer. If resistance of the galvanometer is G , the resistance of ammeter will be:

- (1) $\frac{G}{20}$ (2) $\frac{G}{199}$
 (3) $199 G$ (4) $200 G$

Q14. To measure the temperature coefficient of resistivity α of a semiconductor, an electrical arrangement shown in the figure is prepared. The arm BC is made up of the semiconductor. The experiment is being conducted at 25°C and resistance of the semiconductor arm is $3 \text{ m}\Omega$. Arm BC is cooled at a constant rate of 2°C s^{-1} . If the galvanometer G shows no deflection after 10 s , then α is:



- (1) $-2 \times 10^{-2} ^\circ\text{C}^{-1}$ (2) $-1.5 \times 10^{-2} ^\circ\text{C}^{-1}$
 (3) $-1 \times 10^{-2} ^\circ\text{C}^{-1}$ (4) $-2.5 \times 10^{-2} ^\circ\text{C}^{-1}$

Q15. A transformer has an efficiency of 80% and works at 10 V and 4 kW . If the secondary voltage is 240 V , then the current in the secondary coil is:

- (1) 1.59 A (2) 13.33 A
 (3) 1.33 A (4) 15.1 A

Q16. If frequency of electromagnetic wave is 60 MHz and it travels in air along z direction then the corresponding electric and magnetic field vectors will be mutually perpendicular to each other and the wavelength of the wave in m is :

- (1) 2.5 (2) 10
 (3) 5 (4) 2

Q17. A microwave of wavelength 2.0 cm falls normally on a slit of width 4.0 cm . The angular spread of the central maxima of the diffraction pattern obtained on a screen 1.5 m away from the slit, will be:

- (1) 30° (2) 15°
 (3) 60° (4) 45°

Q18. Monochromatic light of frequency $6 \times 10^{14} \text{ Hz}$ is produced by a laser. The power emitted is $2 \times 10^{-3} \text{ W}$. How many photons per second on an average, are emitted by the source?

(Given $h = 6.63 \times 10^{-34} \text{ J s}$)

- (1) 9×10^{18} (2) 6×10^{15}
 (3) 5×10^{15} (4) 7×10^{16}

Q19. From the statements given below :

- (A) The angular momentum of an electron in n^{th} orbit is an integral multiple of h .
 (B) Nuclear forces do not obey inverse square law.

- (C) Nuclear forces are spin dependent.
 (D) Nuclear forces are central and charge independent.
 (E) Stability of nucleus is inversely proportional to the value of packing fraction.

Choose the correct answer from the options given below :

- (1) (A), (B), (C), (D) only (2) (A), (C), (D), (E) only
 (3) (A), (B), (C), (E) only (4) (B), (C), (D), (E) only

Q20. Conductivity of a photodiode starts changing only if the wavelength of incident light is less than 660 nm.

The band gap of photodiode is found to be $\frac{x}{8}$ eV. The value of X is:

(Given $h = 6.6 \times 10^{-34}$ J s, $e = 1.6 \times 10^{-19}$ C)

- (1) 15 (2) 11
 (3) 13 (4) 21

Q21. A particle initially at rest starts moving from reference point $x = 0$ along x -axis, with velocity v that varies as $v = 4\sqrt{x}$ m s⁻¹. The acceleration of the particle is _____ m s⁻².

Q22. A uniform rod AB of mass 2 kg and Length 30 cm at rest on a smooth horizontal surface. An impulse of force 0.2 N s is applied to end B. The time taken by the rod to turn through at right angles will be $\frac{\pi}{x}$ s, where $x =$ _____.

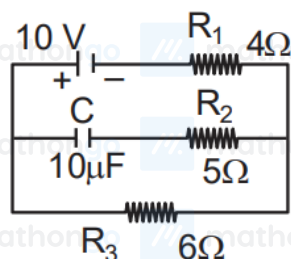
Q23. One end of a metal wire is fixed to a ceiling and a load of 2 kg hangs from the other end. A similar wire is attached to the bottom of the load and another load of 1 kg hangs from this lower wire. Then the ratio of longitudinal strain of upper wire to that of the lower wire will be

[Area of cross section of wire = 0.005 cm², $Y = 2 \times 10^{11}$ N m⁻² and $g = 10$ m s⁻²]

Q24. A mass m is suspended from a spring of negligible mass and the system oscillates with a frequency f_1 . The frequency of oscillations if a mass $9m$ is suspended from the same spring is f_2 . The value of $\frac{f_1}{f_2}$ is _____.

Q25. Suppose a uniformly charged wall provides a uniform electric field of 2×10^4 N C⁻¹ normally. A charged particle of mass 2 g being suspended through a silk thread of length 20 cm and remain stayed at a distance of 10 cm from the wall. Then the charge on the particle will be $\frac{1}{\sqrt{x}} \mu\text{C}$ where $x =$ _____ [use $g = 10$ m s⁻²]

Q26. In an electrical circuit drawn below the amount of charge stored in the capacitor is _____ μC .



Q27. A moving coil galvanometer has 100 turns and each turn has an area of 2.0 cm². The magnetic field produced by the magnet is 0.01 T and the deflection in the coil is 0.05 radian when a current of 10 mA is

passed through it. The torsional constant of the suspension wire is $x \times 10^{-5}$ N - m / rad . The value of x is _____ .

Q28. A coil of 200 turns and area 0.20 m^2 is rotated at half a revolution per second and is placed in uniform magnetic field of 0.01 T perpendicular to axis of rotation of the coil. The maximum voltage generated in the coil is $\frac{2\pi}{\beta}$ volt. The value of β is _____.

Q29. In Young's double slit experiment, monochromatic light of wavelength 5000 \AA is used. The slits are 1.0 mm apart and screen is placed at 1.0 m away from slits. The distance from the centre of the screen where intensity becomes half of the maximum intensity for the first time is _____ $\times 10^{-6} \text{ m}$.

Q30. A particular hydrogen - like ion emits the radiation of frequency $3 \times 10^{15} \text{ Hz}$ when it makes transition from $n = 2$ to $n = 1$. The frequency of radiation emitted in transition from $n = 3$ to $n = 1$ is $\frac{x}{9} \times 10^{15} \text{ Hz}$, when $x =$ _____.

Q31. The number of radial node/s for $3p$ orbital is:

- | | |
|-------|-------|
| (1) 1 | (2) 4 |
| (3) 2 | (4) 3 |

Q32. Given below are two statements :

Statement (I) : Both metal and non-metal exist in s and d -block elements.

Statement (II) : Non-metals have higher ionisation enthalpy and higher electronegativity than the metals.

In the light of the above statements, choose the most appropriate answer from the option given below:

- | | |
|---|---|
| (1) Both Statement I and Statement II are false | (2) Statement I is false but Statement II is true |
| (3) Statement I is true but Statement II is false | (4) Both Statement I and Statement II are true |

Q33. Given below are two statements :

Statement (I) : A π bonding MO has lower electron density above and below the inter-nuclear axis.

Statement (II) : The π^* antibonding MO has a node between the nuclei.

In light of the above statements, choose the most appropriate answer from the options given below:

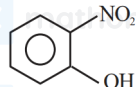
- | | |
|---|---|
| (1) Both Statement I and Statement II are false | (2) Both Statement I and Statement II are true |
| (3) Statement I is false but Statement II is true | (4) Statement I is true but Statement II is false |

Q34. Select the compound from the following that will show intramolecular hydrogen bonding.

(1) H_2O

(2) NH_3

(3) $\text{C}_2\text{H}_5\text{OH}$

(4) 

Q35. Solubility of calcium phosphate (molecular mass, M) in water is W_g per 100 mL at 25°C . Its solubility product at 25°C will be approximately.

- (1) $10^{\frac{7W^3}{M}}$
- (3) $10^{\frac{3W^5}{M}}$

- (2) $10^{\frac{7W^5}{M}}$
- (4) $10^{\frac{5W^5}{M}}$

Q36. Match List - I with List - II.

List - I Compound

List-II Use

- | | |
|--------------------------|---|
| (A) Carbon tetrachloride | (I) Paint remover |
| (B) Methylene chloride | (II) Refrigerators and air conditioners |
| (C) DDT | (III) Fire extinguisher |
| (D) Freons | (IV) Non Biodegradable insecticide |

Choose the correct answer from the options given below:

- | | |
|---|--|
| (1) (A)-(I), (B), (II), (C)-(III), (D)-(IV) | (2) (A)-(III), (B)-(I), (C)-(IV), (D)-(II) |
| (3) (A)-(IV), (B)-(III), (C)-(II), (D)-(I) | (4) (A)-(II), (B)-(III), (C)-(I), (D)-(IV) |

Q37. Given below are two statements:

Statement (I) : SiO_2 and GeO_2 are acidic while SnO and PbO are amphoteric in nature.

Statement (II) : Allotropic forms of carbon are due to property of catenation and $p\pi - d\pi$ bond formation.

In the light of the above statements, choose the most appropriate answer from the options given below:

- | | |
|---|--|
| (1) Both Statement I and Statement II are false | (2) Both Statement I and Statement II are true |
| (3) Statement I is true but Statement II is false | (4) Statement I is true but Statement II is true |

Q38. Which among the following has highest boiling point?

- | | |
|--|--|
| (1) $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_3$ | (2) $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_2 - \text{OH}$ |
| (3) $\text{CH}_3\text{CH}_2\text{CH}_2\text{CHO}$ | (4) $\text{H}_5\text{C}_2 - \text{O} - \text{C}_2\text{H}_5$ |

Q39. The set of meta directing functional groups from the following sets is:

- | | |
|---|--|
| (1) $-\text{CN}$, $-\text{NH}_2$, $-\text{NHR}$, $-\text{OCH}_3$ | (2) $-\text{NO}_2$, $-\text{NH}_2$, $-\text{COOH}$, $-\text{COOR}$ |
| (3) $-\text{NO}_2$, $-\text{CHO}$, $-\text{SO}_3\text{H}$, $-\text{COR}$ | (4) $-\text{CN}$, $-\text{CHO}$, $-\text{NHCOCH}_3$, $-\text{COOR}$ |

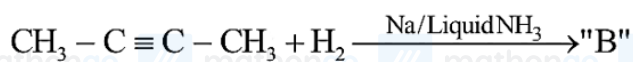
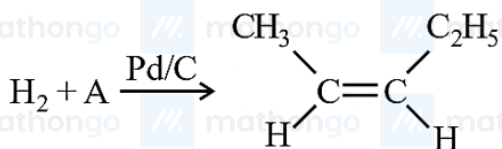
Q40. The functional group that shows negative resonance effect is:

- | | |
|--------------------|------------------|
| (1) $-\text{NH}_2$ | (2) $-\text{OH}$ |
| (3) $-\text{COOH}$ | (4) $-\text{OR}$ |

Q41. Lassaigne's test is used for detection of:

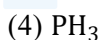
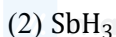
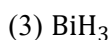
- | | |
|-----------------------------------|--|
| (1) Nitrogen and Sulphur only | (2) Nitrogen, Sulphur and Phosphorous Only |
| (3) Phosphorous and halogens only | (4) Nitrogen, Sulphur, and halogens |

Q42. In the given reactions identify A and B.



- | | |
|--|--|
| (1) A : 2-Pentyne B : trans - 2 - butene | (2) A : n - Pentane B : trans - 2 - butene |
| (3) A : 2 - Pentyne B : Cis - 2 - butene | (4) A : n - Pentane B : Cis - 2 - butene |

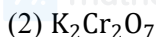
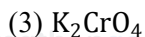
Q43. The strongest reducing agent among the following is:



Q44. The transition metal having highest 3rd ionisation enthalpy is:



Q45. Which of the following compounds show colour due to d - d transition?



Q46. Given below are two statements : one is labelled as Assertion A and the other is labelled as Reason R.

Assertion A : In aqueous solutions Cr^{2+} is reducing while Mn^{3+} is oxidising in nature.

Reason R: Extra stability to half filled electronic configuration is observed than incompletely filled electronic configuration.

In the light of the above statement, choose the most appropriate answer from the options given below:

(1) Both A and R are true and R is the correct explanation of A

(3) A is false but R is true

(2) Both A and R are true but R is not the correct explanation of A

(4) A is true but R is false

Q47. Given below are two statements :

Statement (I) : Dimethyl glyoxime forms a six membered covalent chelate when treated with NiCl_2 solution in presence of NH_4OH .

Statement (II) : Prussian blue precipitate contains iron both in +2 and +3 oxidation states.

In the light of the above statements, choose the most appropriate answer from the options given below:

(1) Statement I is false but Statement II is true

(3) Both Statement I and Statement II are false

(2) Both Statement I and Statement II are true

(4) Statement I is true but Statement II is false

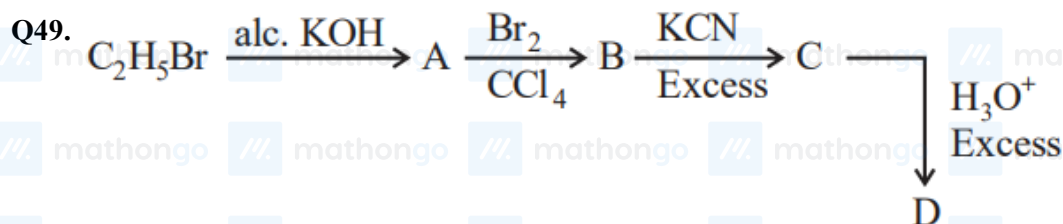
Q48. $\text{CoNH}_3)_6^{3+}$ and CoF_6^{3-} are respectively known as:

(1) Spin free Complex, Spin paired Complex

(3) Outer orbital Complex, Inner orbital Complex

(2) Spin paired Complex, Spin free Complex

(4) Inner orbital Complex, Spin paired Complex



Acid D formed in above reaction is:

(1) Gluconic acid

(3) Oxalic acid

(2) Succinic acid

(4) Malonic acid

Q50. Match List - I with List - II.

List-I (Reactants)

(A) Phenol, Zn / Δ

List-II Products

(I) Salicylaldehyde

(B) Phenol, CHCl_3 , NaOH , HCl

(II) Salicylic acid

(C) Phenol, CO_2 , NaOH , HCl

(III) Benzene

(D) Phenol, Conc. HNO_3

(IV) Picric acid

Choose the correct answer from the options given below.

(1) (A)-(IV), (B)-(II), (C)-(I), (D)-(III)

(2) (A)-(IV), (B)-(I), (C)-(II), (D)-(III)

(3) (A)-(III), (B)-(I), (C)-(II), (D)-(IV)

(4) (A)-(III), (B)-(IV), (C)-(I), (D)-(II)

Q51. 10 mL of gaseous hydrocarbon on combustion gives 40 mL of CO_2 g and 50 mL of water vapour. Total number of carbon and hydrogen atoms in the hydrocarbon is _____.

Q52. For a certain reaction at 300 K, $K = 10$, then ΔG° for the same reaction is $-\text{_____} \times 10^{-1} \text{ kJ mol}^{-1}$.
(Given $R = 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$)

Q53. Following Kjeldahl's method, 1 g of organic compound released ammonia, that neutralised 10 mL of $2\text{M H}_2\text{SO}_4$. The percentage of nitrogen in the compound is _____ %.

Q54. Total number of isomeric compounds (including stereoisomers) formed by monochlorination of 2-methylbutane is _____.

Q55. Mass of ethylene glycol (antifreeze) to be added to 18.6 kg of water to protect the freezing point at -24°C is kg (Molar mass in g mol^{-1} for ethylene glycol 62, K_f of water = $1.86 \text{ K kg mol}^{-1}$)

Q56. The amount of electricity in Coulomb required for the oxidation of 1 mol of H_2O to O_2 is $\text{_____} \times 10^5 \text{ C}$.

Q57. Consider the following redox reaction: $\text{MnO}_4^- + \text{H}^+ + \text{H}_2\text{C}_2\text{O}_4 \rightleftharpoons \text{Mn}^{2+} + \text{H}_2\text{O} + \text{CO}_2$

The standard reduction potentials are given as below E_{red}° $E_{\text{MnO}_4^- / \text{Mn}^{2+}}^\circ = +1.51 \text{ V}$; $E_{\text{CO}_2 / \text{H}_2\text{C}_2\text{O}_4}^\circ = -0.49 \text{ V}$ If the equilibrium constant of the above reaction is given as $K_{\text{eq}} = 10^x$, then the value of $x = \text{_____}$ (nearest integer)

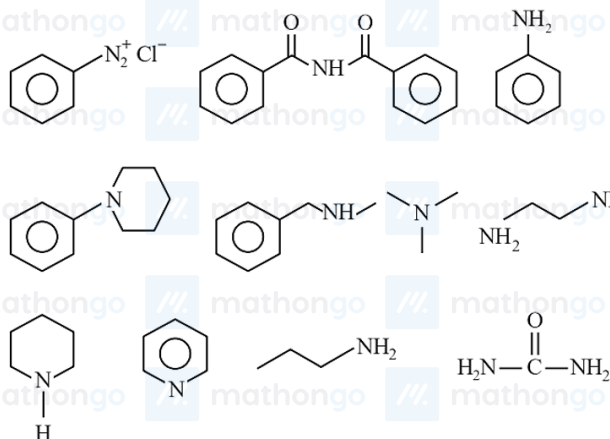
Q58. The following data were obtained during the first order thermal decomposition of a gas A at constant volume:

 $\text{Ag} \rightarrow 2 \text{Bg} + \text{Cg}$

S. No	Time/s	Total pressure/(atm)
1.	0	0.1
2.	115	0.28

The rate constant of the reaction is $\text{_____} \times 10^{-2} \text{ s}^{-1}$ (nearest integer)

Q59. Number of compounds which give reaction with Hinsberg's reagent is _____.



Q60. The number of tripeptides formed by three different amino acids using each amino acid once is _____.

Q61. Let α and β be the roots of the equation $px^2 + qx - r = 0$, where $p \neq 0$. If p , q and r be the consecutive terms of a non-constant G.P and $\frac{1}{\alpha} + \frac{1}{\beta} = \frac{3}{4}$, then the value of $\alpha - \beta^2$ is:

- (1) $\frac{80}{9}$ (2) 9
(3) $\frac{20}{3}$ (4) 8

Q62. If z is a complex number such that $|z| \leq 1$, then the minimum value of $z + \frac{1}{2}3 + 4i$ is:

- (1) 2 (2) $\frac{5}{2}$
(3) $\frac{3}{2}$ (4) 3

Q63. Let S_n denote the sum of the first n terms of an arithmetic progression. If $S_{10} = 390$ and the ratio of the tenth and the fifth terms is $15 : 7$, then $S_{15} - S_5$ is equal to:

- (1) 800 (2) 890
(3) 790 (4) 690

Q64. Let m and n be the coefficients of seventh and thirteenth terms respectively in the expansion of $\frac{1}{3}x^{\frac{1}{3}} + \frac{1}{2x^{\frac{2}{3}}}$.

Then $\frac{n}{m}$ is:

- (1) $\frac{4}{9}$ (2) $\frac{1}{9}$
(3) $\frac{1}{4}$ (4) $\frac{9}{4}$

Q65. The number of solutions of the equation $4\sin^2 x - 4\cos^3 x + 9 - 4\cos x = 0$; $x \in -2\pi, 2\pi$ is:

- (1) 1 (2) 3
(3) 2 (4) 0

Q66. Let the locus of the mid points of the chords of circle $x^2 + y^2 - 1^2 = 1$ drawn from the origin intersect the line $x + y = 1$ at P and Q . Then, the length of PQ is:

- (1) $\frac{1}{\sqrt{2}}$ (2) $\sqrt{2}$
(3) $\frac{1}{2}$ (4) 1

Q67. Let P be a point on the ellipse $\frac{x^2}{9} + \frac{y^2}{4} = 1$. Let the line passing through P and parallel to y -axis meet the circle $x^2 + y^2 = 9$ at point Q such that P and Q are on the same side of the x -axis. Then, the eccentricity of

the locus of the point R on PQ such that $PR:RQ = 4:3$ as P moves on the ellipse, is:

- (1) $\frac{11}{19}$ (2) $\frac{13}{21}$
 (3) $\frac{\sqrt{139}}{23}$ (4) $\frac{\sqrt{13}}{7}$

Q68. Let $fx = \begin{cases} x-1, & x \text{ is even,} \\ 2x, & x \text{ is odd,} \end{cases} x \in N$. If for some $a \in N$, $fffa = 21$, then $\lim_{x \rightarrow a^-} \frac{x^3}{a} - \frac{x}{a}$, where t denotes the greatest integer less than or equal to t , is equal to:

- (1) 121 (2) 144
 (3) 169 (4) 225

Q69. Consider 10 observation x_1, x_2, \dots, x_{10} , such that $\sum_{i=1}^{10} x_i - \alpha = 2$ and $\sum_{i=1}^{10} x_i - \beta^2 = 40$, where α, β are positive integers. Let the mean and the variance of the observations be $\frac{6}{5}$ and $\frac{84}{25}$ respectively. The $\frac{\beta}{\alpha}$ is equal to:

- (1) 2 (2) $\frac{3}{2}$
 (3) $\frac{5}{2}$ (4) 1

Q70. Consider the relations R_1 and R_2 defined as $aR_1b \Leftrightarrow a^2 + b^2 = 1$ for all $a, b \in R$ and $a, bR_2c, d \Leftrightarrow a + d = b + c$ for all $a, b, c, d \in N \times N$. Then

- (1) Only R_1 is an equivalence relation (2) Only R_2 is an equivalence relation
 (3) R_1 and R_2 both are equivalence relation (4) Neither R_1 nor R_2 is an equivalence relation

Q71. Let the system of equations $x + 2y + 3z = 5, 2x + 3y + z = 9, 4x + 3y + \lambda z = \mu$ have infinite number of solutions. Then $\lambda + 2\mu$ is equal to:

- (1) 28 (2) 17
 (3) 22 (4) 15

Q72. If the domain of the function $fx = \frac{\sqrt{x^2 - 25}}{4 - x^2} + \log_{10} x^2 + 2x - 15$ is $-\infty, \alpha \cup \beta, \infty$, then $\alpha^2 + \beta^3$ is equal to:

- (1) 140 (2) 175
 (3) 150 (4) 125

Q73. Let $fx = 2x^2 + 5x - 3, x \in R$. If m and n denote the number of points where f is not continuous and not differentiable respectively, then $m + n$ is equal to:

- (1) 5 (2) 2
 (3) 0 (4) 3

Q74. The value of $\int_0^1 2x^3 - 3x^2 - x + 1^{\frac{1}{3}} dx$ is equal to:

- (1) 0 (2) 1
 (3) 2 (4) -1

Q75. If $\int_0^{\frac{\pi}{3}} \cos^4 x dx = a\pi + b\sqrt{3}$, where a and b are rational numbers, then $9a + 8b$ is equal to:

- (1) 2 (2) 1
 (3) 3 (4) $\frac{3}{2}$

Q76. Let α be a non-zero real number. Suppose $f: R \rightarrow R$ is a differentiable function such that $f0 = 1$ and $\lim_{x \rightarrow -\infty} fx = 1$. If $f'x = \alpha fx + 3$, for all $x \in R$, then $f - \log_e 2$ is equal to _____.

(1) 1

(3) 9

(2) 5

(4) 7

Q77. Consider a ΔABC where $A(1, 3, 2)$, $B(-2, 8, 0)$ and $C(3, 6, 7)$. If the angle bisector of $\angle BAC$ meets the line BC at D , then the length of the projection of the vector \vec{AD} on the vector \vec{AC} is:

(1) $\frac{37}{2\sqrt{38}}$ (3) $\frac{39}{2\sqrt{38}}$ (2) $\frac{\sqrt{38}}{2}$ (4) $\sqrt{19}$

Q78. If the mirror image of the point $P(3, 4, 9)$ in the line $\frac{x-1}{3} = \frac{y+1}{2} = \frac{z-2}{1}$ is α, β, γ , then $14\alpha + \beta + \gamma$ is:

(1) 102

(3) 108

(2) 138

(4) 132

Q79. Let P and Q be the points on the line $\frac{x+3}{8} = \frac{y-4}{2} = \frac{z+1}{2}$ which are at a distance of 6 units from the point $R(1, 2, 3)$. If the centroid of the triangle PQR is α, β, γ , then $\alpha^2 + \beta^2 + \gamma^2$ is:

(1) 26

(3) 18

(2) 36

(4) 24

Q80. Let Ajay will not appear in JEE exam with probability $p = \frac{2}{7}$, while both Ajay and Vijay will appear in the exam with probability $q = \frac{1}{5}$. Then the probability, that Ajay will appear in the exam and Vijay will not appear is:

(1) $\frac{9}{35}$ (3) $\frac{24}{35}$ (2) $\frac{18}{35}$ (4) $\frac{3}{35}$

Q81. The lines L_1, L_2, \dots, L_{20} are distinct. For $n = 1, 2, 3, \dots, 10$ all the lines L_{2n-1} are parallel to each other and all the lines L_{2n} pass through a given point P . The maximum number of points of intersection of pairs of lines from the set L_1, L_2, \dots, L_{20} is equal to:

Q82. If three successive terms of a G.P. with common ratio $r > 1$ are the length of the sides of a triangle and r denotes the greatest integer less than or equal to r , then $3r + -r$ is equal to:

Q83. Let ABC be an isosceles triangle in which A is at $(-1, 0)$, $\angle A = \frac{2\pi}{3}$, $AB = AC$ and B is on the positive x -axis. If $BC = 4\sqrt{3}$ and the line BC intersects the line $y = x + 3$ at α, β , then $\frac{\beta^4}{\alpha^2}$ is:

Q84. Let $A = I_2 - 2MM^T$, where M is real matrix of order 2×1 such that the relation $M^T M = I_1$ holds. If λ is a real number such that the relation $AX = \lambda X$ holds for some non-zero real matrix X of order 2×1 , then the sum of squares of all possible values of λ is equal to:

Q85. If $y = \frac{\sqrt{x+1}x^2 - \sqrt{x}}{x\sqrt{x} + x + \sqrt{x}} + \frac{1}{15}3\cos^2 x - 5\cos^3 x$, then $96y' \frac{\pi}{6}$ is equal to:

Q86. Let $f: 0, \infty \rightarrow R$ and $Fx = \int_0^x t f(t) dt$. If $Fx^2 = x^4 + x^5$, then $\sum_{r=1}^{12} f(r^2)$ is equal to:

Q87. Three points $O(0, 0)$, $P(a, a^2)$, $Q(-b, b^2)$, $a > 0$, $b > 0$, are on the parabola $y = x^2$. Let S_1 be the area of the region bounded by the line PQ and the parabola, and S_2 be the area of the triangle OPQ . If the minimum value of $\frac{S_1}{S_2}$ is $\frac{m}{n}$, $\gcd(m, n) = 1$, then $m + n$ is equal to:

Q88. The sum of squares of all possible values of k , for which area of the region bounded by the parabolas $2y^2 = kx$ and $ky^2 = 2y - x$ is maximum, is equal to:

Q89. If $\frac{dx}{dy} = \frac{1+x-y^2}{y}$, $x_1 = 1$, then $5x_2$ is equal to:

Q90. Let $\vec{a} = \hat{i} + \hat{j} + \hat{k}$, $\vec{b} = -\hat{i} - 8\hat{j} + 2\hat{k}$ and $\vec{c} = 4\hat{i} + c_2\hat{j} + c_3\hat{k}$ be three vectors such that $\vec{b} \times \vec{a} = \vec{c} \times \vec{a}$. If the angle between the vector \vec{c} and the vector $3\hat{i} + 4\hat{j} + \hat{k}$ is θ , then the greatest integer less than or equal to $\tan^2 \theta$ is:

ANSWER KEYS

1. (3)	2. (3)	3. (4)	4. (3)	5. (3)	6. (1)	7. (4)	8. (4)
9. (2)	10. (1)	11. (4)	12. (1)	13. (1)	14. (3)	15. (2)	16. (3)
17. (3)	18. (3)	19. (3)	20. (1)	21. (8)	22. (4)	23. (3)	24. (3)
25. (3)	26. (60)	27. (4)	28. (5)	29. (125)	30. (32)	31. (1)	32. (2)
33. (3)	34. (4)	35. (2)	36. (2)	37. (3)	38. (2)	39. (3)	40. (3)
41. (4)	42. (1)	43. (3)	44. (2)	45. (1)	46. (1)	47. (1)	48. (2)
49. (2)	50. (3)	51. (14)	52. (57)	53. (56)	54. (6)	55. (15)	56. (2)
57. (338)	58. (2)	59. (5)	60. (6)	61. (1)	62. (3)	63. (3)	64. (4)
65. (4)	66. (1)	67. (4)	68. (2)	69. (1)	70. (2)	71. (2)	72. (3)
73. (4)	74. (1)	75. (1)	76. (1)	77. (1)	78. (3)	79. (3)	80. (2)
81. (101)	82. (1)	83. (36)	84. (2)	85. (105)	86. (219)	87. (7)	88. (8)
89. (5)	90. (38)						